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# Alloy Materials for Plasmonic Refractive Index Sensing

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We have numerically investigated the plasmonic refractive index sensor capabilities of Au–Ag–Cu alloys using experimentally determined permittivity values. Calculations were performed by simulating the typical Kretschmann configuration of surface plasmon polariton (SPR) excitation, as well as the localized surface plasmon resonance (LSPR) of nanoparticles. Sensor performance was evaluated as the response to changes in the refractive index of the surrounding environment as well as the attainable separation of peaks. By considering not only the peak shift, but also the spectral separation, SPR and LSPR sensors can be discussed on equal terms. In studies of both SPR and LSPR, specific alloy configurations were found to be superior to pure gold.

#### 1. Introduction

Plasmons represent a set of optical phenomena caused by the resonance between oscillations of the electromagnetic field of incident light and collective oscillations of free electrons. When the term plasmonic materials is invoked in the visible wavelength range, we generally mean metals, in particular gold, silver, and copper.

However, for numerous applications, there is a distinct need to broaden the range of plasmonic materials and, by extension, their properties through alloying methods. Chemical synthesis is just one example of a particularly rapid way of creating various plasmonic nanoparticles.<sup>(1-7)</sup>

When estimating the optical properties of alloys, weighted averaging of the constants associated with the constituent pure metals is often attempted; however, the results are often inconsistent with observations. We first demonstrated the importance of experimental determinations of the optical constants/permittivity of metals  $(n = n + ik, \varepsilon = \varepsilon_1 + i\varepsilon_2 = n^2 - k^2 + 2ink)$ . (8,9)

Subsequently, numerous research groups published the results of their alloy permittivity measurements. (10-12) It was shown that optical properties were strongly dependent on the deposition method employed, and, by extension, on the resulting extent of structural order (such as the degree of crystallinity, phase separation). This was illustrated in the recent experimental investigation of permittivity in 38 variations of the Au-Ag-Cu alloy system. (13) Furthermore,

\*Corresponding author: e-mail: nishijima-yoshiaki-sp@ynu.ac.jp http://dx.doi.org/10.18494/SAM.2017.1582 optical permittivity data can be used to predict the surface plasmon polariton (SPR)/localized surface plasmon resonance (LSPR) sensing properties of a metal.

In this study, we numerically calculated Au–Ag–Cu alloy metal SPR and LSPR properties and estimated their variations in response to changes in the refractive index of the surrounding environment. In each case, calculations were based on experimentally determined alloy permittivity values. Furthermore, since in most other publications, only the resonance peak shift per refractive index unit (RIU) change is considered, performance comparisons between angular-dependence-based SPR sensors and wavelength-shift-dependence-based LSPR sensors are made difficult.<sup>(14–16)</sup>

However, the separation between two peaks can be used to draw comparisons between the two different methods. Consequently, we also discuss the sensing performance of SPR/LSPR sensors on the basis of their unified figures of merit (FOMs).

## 2. Samples and Methods

Numerical calculations of the SPR/LSPR sensor response have been performed using experimentally determined values of optical properties of the 38 different Au–Ag–Cu metal alloys published previously. (13) Therein, optical constants were deduced by subjecting three different thickness layers for each of the alloys to measurements of the transmittance and reflectance spectra.

SPR can be induced on a flat metal film via the evanescent coupling of light. Most common methods of achieving this in SPR sensors involve the use of total internal reflection in a prism. Two types of surface plasmon excitation geometries, which use prisms, are known as Otto and Kretshmann configurations.

Since the Otto geometry requires a controlled nanometer-scale air gap between the prism and a thin metal film, the significantly simpler Kretshmann configuration is a more prevalent realization of SPR sensing. Usually, the SPR excitation angle is approximately expressed as

$$\sin \theta \sim \frac{n_s}{n_p},\tag{1}$$

where  $n_s$  is the refractive index of the sensing layer, and  $n_p$  is the refractive index of the prism. A rigorous expression for the asymmetric curve-fitting equation of a Kretshmann SPR sensor, derived from Fresnel equations for each of the layers (air, metal, and prism), was reported by Kurihara *et al.*<sup>(17)</sup> This expression was used to simulate SPR in this work.

Obtaining stable SPR performance comparisons between the near-infrared excitation of the alloys is preferable, since both Au and Cu have absorption losses due to interband transitions in the spectral region below 600 nm. For this reason, the wavelength of incident light was set at 800 nm. Furthermore, the metal film thickness was set to 50 nm. For film thicknesses below 30 nm (almost the same order as the skin depth of a metal), absorption losses become excessive. Conversely, above 70 nm thickness, reflection at the prism/metal interface becomes larger as light can no longer penetrate to the metal/air interface.

For numerical simulation of LSPR on spherical nanoparticles, absorption and scattering cross sections were obtained using the following equations. (18)

$$\sigma_{abs} = k \operatorname{Im}(\alpha)$$

$$\sigma_{sca} = \frac{k^4}{6\pi} |\alpha^2|$$

$$\alpha = 4\pi r^3 \frac{(\varepsilon_1 - \varepsilon_s)(\varepsilon_1 + 2\varepsilon_s) + (\varepsilon_2)^2 + i3\varepsilon_2\varepsilon_s}{(\varepsilon_1 + 2\varepsilon_s)^2 + (\varepsilon_2)^2}$$

$$k = \frac{2\pi \sqrt{\varepsilon_s}}{\lambda}$$
(2)

Here,  $\varepsilon_s$  is the permittivity of the surrounding medium (=  $n_s^2$ , square of refractive index of the surrounding medium) and r is the diameter of the particle. The diameter of the nanosphere was set to 30 nm. For particles, below 10 nm in diameter, the refractive index of the bulk alloy metal is no longer applicable and  $\varepsilon_1$  and  $\varepsilon_2$  become larger than would be observed in thin film.

For both SPR and LSPR sensor calculations, the surrounding refractive index change varied from 1.0 (air) to 1.4 (typical for organic solvents such as ethylene glycol).

### 3. Results and Discussion

Figure 1(a) shows the angular dependence of the reflectance associated with SPR excitation in air (*n* = 1) in the Kretshmann geometry. As mentioned previously, in these calculations, the excitation wavelength was 800 nm and metal thickness was set at 50 nm. Almost all SPR peaks appeared in the 34 to 35° angle interval, with the minimum reflectance varying between 0.1 and 0.5. Similarly, Fig. 1(b) shows the results of the optical absorbance and scattering cross section spectra calculation for 10 nm metal particles. There is a strong spectral correspondence between both scattering and absorbance cross section peaks. In the Au–Ag–Cu alloy system, LSPR peaks appeared in the wavelength range between 400 and 650 nm. Owing to the general correspondence between the two cross section spectra, the optical property of scattering was chosen for the discussion of LSPR sensing.

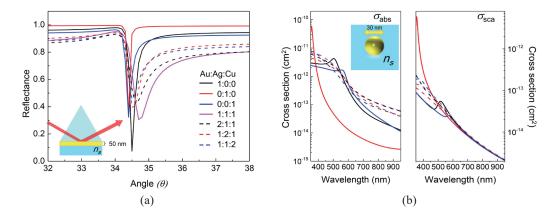


Fig. 1. (Color online) (a) Numerically calculated SPR reflection response in 50-nm-thick films of Au, Ag, Cu, and several of their alloys in the Kretshmann configuration. (b) Numerically calculated spectral dependence of scattering and absorption cross sections of 10 nm nanoparticles of pure Au, Ag, Cu, and several of their alloys.

Figure 2 shows the variations in Au SPR and LSPR calculations caused by changes in the refractive index of the surrounding medium. Both peak angle in SPR and wavelength shift in LSPR increased linearly with increases in the surrounding refractive index. The slope values of  $d\theta/dn$  and  $d\lambda/dn$  are 47.8 and 77.7, respectively, for SPR and LSPR. According to these values, LSPR would appear to exhibit a higher sensitivity than an SPR sensor. However, there is a significant difference between the spectral widths of the plasmon bands of these two systems. SPR has peaks with sharp angular dependence, whereas those of LSPR are very broad. Therefore, "peak separation" is an important aspect when discussing and comparing the resolutions of the two sensing schemes. Peak separation (R) is defined as

$$R = \frac{A_s - A_1}{\frac{1}{2} \times (W_s + W_1)},\tag{3}$$

where A represents the position of the peak maximum either as  $\theta_{max}$  or  $\lambda_{max}$ , and W is the full width at half maximum of the peak. The subscripts s and 1 respectively indicate the value of the refractive index in the surrounding medium and the n=1 condition. The red plot in Figs. 2(b)

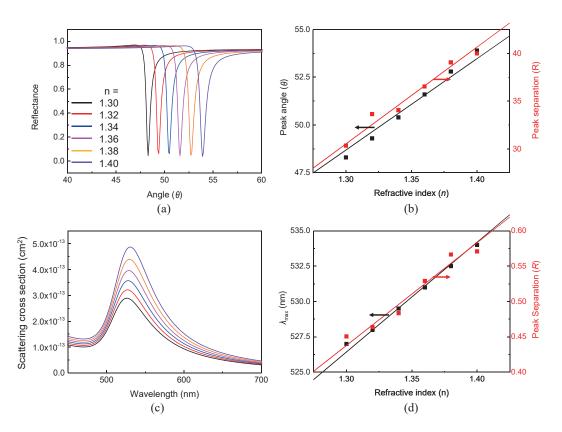


Fig. 2. (Color online) (a) Angular dependence variations of SPR excitation response as a result of changes in the refractive index of the surrounding medium of a 50 nm Au thin film in the Kretshmann configuration. (b) Plot of the peak angular position and peak separation shifts as functions of refractive index. (c) Changes in spectral LSPR scattering cross section of a 10 nm Au nanoparticle as a result of variations in the refractive index of the surrounding environment. (d) LSPR peak wavelength position and peak separation shifts as functions of refractive index.

and 2(d) shows the peak separation of the SPR and LSPR sensors. Naturally, the peak separation also linearly increases with the surrounding refractive index. However, the slopes for these plots are 101 and 1.45 for SPR and LSPR, respectively. In light of this, SPR setups have two orders of magnitude higher resolution than LSPR sensors.

The aforementioned numerical analysis of peak shift and peak separation was subsequently applied to pure Au, Ag, and Cu as well as to 38 different compositions of their alloys. Figure 3 shows the ternary plots of all the alloys, with panel (a) showing the peak shift and panel (b) the peak separation for the SPR configuration, whereas (c) and (d), respectively, give equivalent parameters in the LSPR case. In the case of an SPR sensor, there is a negative correlation between peak shift and peak separation. The maximum  $d\theta/dn$  is observed for alloy compositions around Au<sub>0.6</sub>Ag<sub>0.1</sub>Cu<sub>0.3</sub> and Au<sub>0</sub>Ag<sub>0.4</sub>Cu<sub>0.6</sub>, both of which are superior to pure Au, Ag, and Cu. However, when the peak separation is considered, pure Au, Ag, and Cu perform far better than any of their alloys; among the alloys, Au<sub>0.4</sub>Ag<sub>0.4</sub>Cu<sub>0.2</sub> has the largest peak separation. Conversely, for LSPR sensing, peak shift and peak separation values have a positive correlation and tend to occur simultaneously for a given alloy composition. While pure Au and Ag exhibit large FOM values—

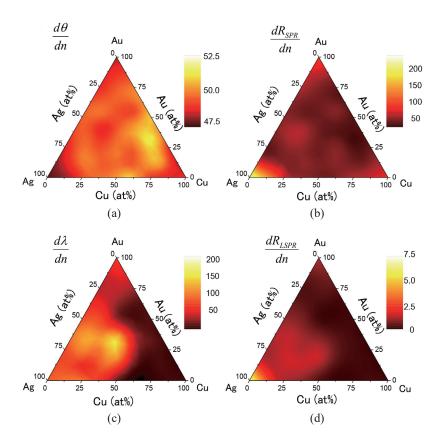


Fig. 3. (Color online) Au–Ag–Cu alloy composition map of refractive index sensing performance FOMs. (a) SPR peak angle shift in the Kretshmann configuration, (b) SPR peak separation, (c) LSPR scattering peak shift for 10 nm nanoparticles, and (d) LSPR peak separation.

Au, 10–50%; Ag, 35–65%; and Cu, 15–40%—composit materials also have values exceeding that of pure Au and Cu. In this composition range, the phase separation of Ag and Cu was suppressed by the presence of Au. (13) A totally homogeneous alloy could be obtained. From these results, the specific compositions of alloy metals have significant potential for use in SPR or LSPR sensor applications.

Of course, the technical realization of a given sensing scheme heavily affects the attainable resolution. For instance, spectrometer resolution among other factors depends on optical setup, grating, and focal length. A small spectrometer (for example, USB2000, Ocean Photonics, Co. or Minispectrometer and PMA-12, Hamamatsu Photonics Co.) has a wavelength resolution of around 3–7 nm. On the other hand, a long-focal-length spectrometer with a CCD detector can reach resolutions above 0.1 nm (1000M II; Horiba Scientific Co. or Spectra Pro SP2750; Princetone Instruments Co.).

The peak shift or peak separation are very important to know the physical or chemical meaning of the sensing principle. However, it is difficult to compare the different sensing devices. For example, SPR and LSPR are measured physical quantities that are different from each other. The FOM of a sensing device is an artificial parameter for the comparative evaluation of performance. Sometimes, for particular applications, FOMs different from the usual device sensitivity, such as the footprint, weight, price of system, maintenance cost, or power consumption, must be considered. In particular, stationary versus portable sensing devices tend to exhibit contrasting FOMs. Similarly, SPR and LSPR sensor system design may be guided by considerations beyond sensitivity.

#### 4. Conclusions

In this study, we numerically demonstrate the sensing performances of SPR and LSPR schemes that use the Au–Ag–Cu alloy system based on experimentally determined values of optical permittivity. Some metal alloy compositions exhibit performance superior to their pure versions, especially Au and Cu. In this way, alloys provide properties beyond that of their constituent components as well as additional new functions (catalytic, hydrogen storage, shape memory, magnetic, and others). The SPR/LSPR sensing field has matured and practical use will experience rapid progress. As the application field broadens, it will be necessary to design sensor systems with application-oriented FOMs.

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